

# Planning under Uncertainty with Action Languages

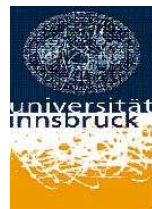
## *A Logic Programming Approach*

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# Overview

- Introduction
- Answer Set Programming in a nutshell
- Planning in Logic Programming (an adhoc solution).
- Planning & Knowledge Representation in Action Language  $\mathcal{K}$ ,
  - Syntax & Semantics
  - Knowledge State vs. World State Encodings
- (short) Translations to LP, the  $DLV^{\mathcal{K}}$  Planning System

# Introduction

What is Planning?

- Start: **initial situation** (or **state**)
- Desired: reach a **goal**
- At disposal: **actions**

**Problem:** Find a suitable sequence of actions (a **plan**) whose execution brings about the goal.

# Planning and AI

Planning is a challenging problem for AI since 1950's  
McCarthy: Missionaries and Cannibals (1959)

- Logic-based approaches
- Heuristic search methods
- ad hoc approaches
- Graphplan
- Planning as Model-Checking
- ...
- Planning as Satisfiability (SAT Planning)
- Answer Set Planning (Planning using Answer Set Programming)

# Answer Set Programming in a nutshell

Classical logic Programming extended with

- Disjunction
- Default negation
- Strong (classical) negation
- Integrity constraints
- No function symbols (finiteness)

# Answer Set Programming: Idea

- Fundamental concept:  
**Models, not proofs, represent solutions!**
- Need techniques to **compute models** (not to compute proofs)

What is this good for?

Solve *search problems*

Compute, e.g., one/all solutions of the N-queens problem,  
SAT, one/all routes to reach the airport; . . . **compute plans!**

# ASP: Syntax

Rules:

$a_1 \vee \dots \vee a_n \text{ :- } b_1, \dots, b_k, \text{ not } b_{k+1}, \dots, \text{ not } b_l.$

Constraints:  $\text{ :- } b_1, \dots, b_k, \text{ not } b_{k+1}, \dots, b_l.$

- $a$ s and  $b$ s are atoms ( $p$ ) or strongly negated atoms ( $\neg p$ )
- variables are allowed in arguments of atoms
- a **program** is a set of rules and constraints
- order of literals and rules does not matter

```
interested(X) v curious(X) :- attendsTalk(X).  
attendsTalk(X) :- staff(X), not onVacation(X).
```

# Answer Set Semantics 1/2

Let  $M$  be a (consistent) set of literals

A Rule

$a_1 \vee \dots \vee a_n :- b_1, \dots, b_k, \text{not } b_{k+1}, \dots, \text{not } b_l.$

is called **satisfied** wrt.  $M$  iff:

If  $b_1, \dots, b_k \in M$  and  $b_{k+1}, \dots, b_l \notin M$  then

at least one of  $a_1, \dots, a_n \in M$ .



# Answer Set Semantics 2/2

- $P$  — logic program
- $M$  — (consistent) set of literals
- *Reduct*  $P^M$  (Gelfond, Lifschitz)
  - for each  $l \in M$  remove rules with `not`  $l$  in the body
  - remove literals `not`  $l$  from all other rules
- $M$  is called answer set iff it is a **minimal** set such that all rules of  $P^M$  are satisfied wrt.  $M$

# Example 1 – Positive Program

```
interested(you) v curious(you) :- attendsTalk(you).  
attendsTalk(you).
```

M1 = {attendsTalk(you), curious(you)} (Answer Set)

M2 = {attendsTalk(you), interested(you)} (Answer Set)

M3 = {attendsTalk(you)} (first rule not satisfied)

M4 = {attendsTalk(you), interested(you), curious(you)} (not minimal)

# Example 2 – Constraints

Constraints “prohibit” Answer Sets:

```
interested(you) v curious(you) :- attendsTalk(you) .  
attendsTalk(you) .  
:- bored(you), interested(you) .  
bored(you) .
```

Only one answer set:

```
M = {attendsTalk(you), curious(you), bored(you)}
```

# Example 3 – Default Negation

```
interested(you) :- not sleepy(you).
```

```
M = {interested(you)}
```

# Example 4 – Default Negation

`interested(you) :- not sleepy(you) .`

`sleepy(you) .`

`M = {sleepy(you) }`

**Nonmonotonic Reasoning!**

# Example 5 – Default Negation

`interested(you) :- not sleepy(you).`

`sleepy(you) :- not interested(you).`

`M1 = {sleepy(you)}`

`M2 = {interested(you)}`

# Example 6 – Strong Negation

```
interested(you) :- not -interested(you).
```

```
-interested(you) :- not interested(you).
```

```
M1 = {-interested(you)}
```

```
M2 = {interested(you)}
```

Literals can be *true*, *false* or *unknown* in an answer set if the literal appears in positive and negative form!

# Answer Set Planning

First attempt: adhoc encoding

**Idea:** Use expressiveness of Answer Set Semantics for guessing plans.

- NP ( $\Sigma_2^P = \text{NP}^{\text{NP}}$ ) for normal (disjunctive) logic programs

**Method:** (by e.g. Subrahmanian & Zaniolo, Dimopoulos et al., Lifschitz . . . . .)

- Formulate planning problem as a logic program  $\Pi$  (describe trajectories)
- Compute any answer sets (i.e. models) of  $\Pi$ , which encode possible plans.

**Advantage:** Declarative problem solving

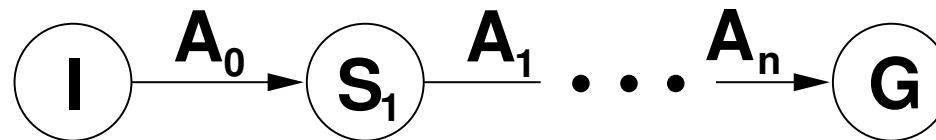


# High-level View

**Input:** Fluents (state variables)  $F$   
Actions (that usually modify fluents)  $A$   
Initial state  $I$ , goal state  $G$   
State constraints, action descriptions

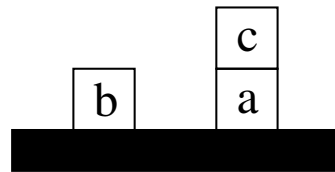
**Evolution:** Discrete steps of time (stages),  $0, 1, \dots, n$

**Output:** A sequence of *action sets* (or single actions)  
 $\langle A_0, A_1, \dots, A_n \rangle$  which transforms  $I$  into  $G$

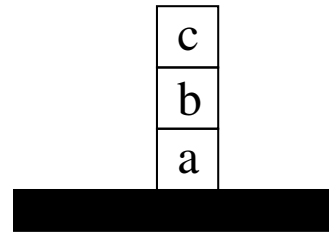


# Example: Blocks World

initial:



goal:



**Actions:** Move a block from one location to another (`move(b, a)`, ...)

**Fluents:** Predicates describing the state (`clear(b, 0)`, `on(c, a, 0)`, ...))

# Example: Blocks World

Background Knowledge:

```
block(a). block(b). block(c).
```

```
location(X):- block(X). location(table).
```

Use discrete time 0,1,2,... Here: 3 Steps

```
act_time(0). act_time(1). act_time(2).
```

% 3 time stamps

# Example: Blocks World

Background Knowledge:

```
block(a).  block(b).  block(c).  
location(X):- block(X).  location(table).
```

Use discrete time 0,1,2,... Here: 3 Steps

```
act_time(0). act_time(1). act_time(2).
```

% 3 time stamps

% Initial state:

```
on(a, table, 0).  on(b, table, 0).  on(c, a, 0).
```

% Goal:

```
goal:- on(a, table, 3), on(b, a, 3), on(c, b, 3).
```

```
:- not goal.
```

# Example: Blocks World

Background Knowledge:

```
block(a).  block(b).  block(c).  
location(X):- block(X).  location(table).
```

Use discrete time 0,1,2,... Here: 3 Steps

```
act_time(0). act_time(1). act_time(2). % 3 time stamps
```

% Initial state:

```
on(a, table, 0).  on(b, table, 0).  on(c, a, 0).
```

% Goal:

```
goal:- on(a, table, 3), on(b, a, 3), on(c, b, 3).
```

```
:- not goal.
```

% The meat of the program ...

%Guess: At any action time T, move a block B to some location L or not

```
move(B, L, T) v  - move(B, L, T):- block(B), location(L),  
                                     act_time(T), B != L.
```

% Effects of moving a block: The block is now at the new location...

`on(B, L, T1) :- move(B, L, T), T1 = T + 1.`

% ... and it is no longer at the old location.

`-on(B, L, T1) :- move(B, L1, T), on(B, L, T), T1 = T + 1,  
L1 <> L.`

% Inertia: Unless a block is *known* to be moved, assume it is still at old place.

`on(B, L, T1) :- on(B, L, T), not -on(B, L, T1), T1 = T + 1.`

% Constraints

`:- move(B, L, T), on(_, B, T). % A block can only be moved if it's clear.`

`:- move(B, B1, T), on(_, B1, T), block(B1). % No move onto an occupied block`

`:- move(B, _, T), move(B1, _, T), B != B1. % Move only one block at each step`

`:- move(_, L, T), move(_, L1, T), L != L1. % No move to different locations`

# Disadvantages of the Method

- Ad hoc encoding
- Semantics is implicit in the encoding
- Inflexible (changes, etc)
- ...

# Disadvantages of the Method

- Ad hoc encoding
- Semantics is implicit in the encoding
- Inflexible (changes, etc)
- ...

Better: Provide genuine action / planning language.

- Syntax and first class citizen semantics
- Compile to logic engines (e.g., to Answer Set solvers like `DLV`, `smodels`)



# Planning & Knowledge Representation in Action Language $\mathcal{K}$

# Planning Languages

## Early attempts

- Deductive Planning (Green, 1969)
- Situation Calculus (McCarthy & Hayes, 1969)
- STRIPS (Fikes et al., 1971) + descendants (e.g. PDDL)
- Temporal Logic (McDermott, 1982)
- Event Calculus (Kowalski & Sergot, 1986; Eshghi 1988)
- Fluent Calculus (Thielscher, 2000)
- ...
- Action Languages, e.g.  $\mathcal{A}$ ,  $\mathcal{AR}$ ,  $\mathcal{A}_K$ ,  $\mathcal{C}$ ,  $\mathcal{K}$ ,...

# Action Language $\mathcal{K}$

A relative of action languages  $\mathcal{A}$  (Gelfond & Lifschitz, 1993) and  $\mathcal{C}$  (Giunchiglia & Lifschitz, 1998)

Divide predicates in

- state predicates, further divided in
  - rigid predicates (constants)
  - fluent predicates (variables)
- action predicates (variables)

Formulate axioms about transitions rather than operators like in “classical” planning languages.

# Main Features of $\mathcal{K}$

- Incomplete states (“knowledge states”)
- Default (nonmonotonic) negation and strong (classical) negation
- Typed fluents and actions
- Initial state constraints
- Conditional executability
- Causation rules
- Inertia
- Nondeterministic action effects

# $\mathcal{K}$ Planning Domains and Problems

Background Knowledge  $\Pi$ : A logic program  $\Pi$  with a single model,

(answer set) defining type information and static knowledge.

$\mathcal{K}$  Action Description  $AD$ :

fluents:  $D_F$            % fluent defs  
actions:  $D_A$            % action type defs  
always:  $C_R$            % causation rules + exec. cond's  
initially:  $C_I$            % initial state constraints

$\mathcal{K}$  Planning Domain:  $\langle \Pi, AD \rangle$

$\mathcal{K}$  Planning Problem: additional goal

goal:  $G?(i)$    ground literal(s)  $G$ ; plan length  $i \geq 0$ .

# Blocksworld – $\mathcal{K}$ Representation

## Background knowledge

$$\Pi = \{\text{block}(a). \text{block}(b). \text{block}(c). \\ \text{location}(\text{table}). \\ \text{location}(L) :- \text{block}(L).\}$$

Note: Syntactic and/or other restrictions might help ensure that  $\Pi$  has a single model (answer set).

# Action Description

*AD:*

fluents : on(B,L) requires block(B), location(L).  
occupied(B) requires location(B).

actions : move(B,L) requires block(B), location(L).

always : executable move(B,L) if not occupied(B),  
not occupied(L), B <> L.

inertial on(B,L).  
caused on(B,L) after move(B,L).  
caused – on(B,L1) after move(B,L), on(B,L1), L <> L1.  
caused occupied(B) if on(B1,B), block(B).  
noConcurrency.

initially : on(a, table). on(b, table). on(c, a).

# *AD* – Fluent and Action Type Defs

```
fluents :    on(B,L) requires block(B), location(L).
            occupied(B) requires location(B).
actions :    move(B,L) requires block(B), location(L).
always :     executable move(B,L) if not occupied(B),
            not occupied(L), B <> L.
            inertial on(B,L).
            caused on(B,L) after move(B,L).
            caused - on(B,L1) after move(B,L), on(B,L1), L <> L1.
            caused occupied(B) if on(B1,B), block(B).
            noConcurrency.
initially :  on(a, table). on(b, table). on(c, a).
```



# AD – Action Executability

fluents : `on(B,L)` requires `block(B)`, `location(L)`.

`occupied(B)` requires `location(B)`.

actions : `move(B,L)` requires `block(B)`, `location(L)`.

always : `executable move(B,L) if not occupied(B),  
not occupied(L), B <> L.`

`inertial on(B,L).`

`caused on(B,L) after move(B,L).`

`caused – on(B,L1) after move(B,L), on(B,L1), L <> L1.`

`caused occupied(B) if on(B1,B), block(B).`

`noConcurrency.`

initially : `on(a, table). on(b, table). on(c, a).`

# AD – Transition Rules (Causality)

fluents :    `on(B,L)` requires `block(B)`, `location(L)`.  
              `occupied(B)` requires `location(B)`.

actions :    `move(B,L)` requires `block(B)`, `location(L)`.

always :     `executable move(B,L) if not occupied(B),`  
  `not occupied(L), B <> L.`

`inertial on(B,L).`  
              `caused on(B,L) after move(B,L).`  
              `caused – on(B,L1) after move(B,L), on(B,L1), L <> L1.`  
              `caused occupied(B) if on(B1,B), block(B).`  
              `noConcurrency.`

initially :  `on(a, table). on(b, table). on(c, a).`

*Remark: Causation Rules describe valid transitions rather than operator descriptions in languages like STRIPS or PDDL!*

# *AD* – Initial State Constraints

fluents : on(B,L) requires block(B), location(L).

occupied(B) requires location(B).

actions : move(B,L) requires block(B), location(L).

always : executable move(B,L) if not occupied(B),  
not occupied(L),  $B \neq L$ .

inertial on(B,L).

caused on(B,L) after move(B,L).

caused  $\neg$  on(B,L1) after move(B,L), on(B,L1),  $L \neq L1$ .

caused occupied(B) if on(B1,B), block(B).

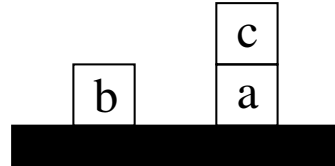
noConcurrency.

initially : on(a,table). on(b,table). on(c,a).

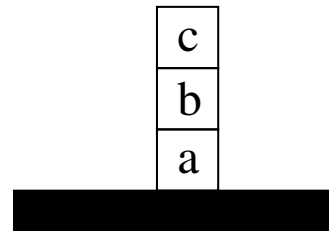
# Goal

goal : on(c, b), on(b, a), on(a, table)?(3)

initial:



goal:



Intuitively: Feasible plan is

move(c, table); move(b, a); move(c, b)

# Features 1/3:

## ● Qualification Problem:

Overriding by exceptions to executability

```
executable act if < cond1 >
```

```
nonexecutable act if < cond2 >
```

Example:

```
executable move(B, L) if B != L.
```

```
nonexecutable move(B, L) if occupied(B).
```

```
nonexecutable move(B, L) if occupied(L).
```

# Features 2/3

- **Frame Problem/Inertia:**

`inertial on(B, L).`

short for

`caused on(B, L) if not – on(B, L) after on(B, L).`

- **Uncertainty: in general by unstratified negation.**

`total loaded(gun).`

short for

`caused loaded(gun) if not – loaded(gun).`

`caused – loaded(gun) if not loaded(gun).`

# Features 3/3

- Ramifications/State Axioms:

Simple by causal rules:

`caused supported(B1) if on(B1, table).`

`caused supported(B1) if on(B1, B2), supported(B2).`

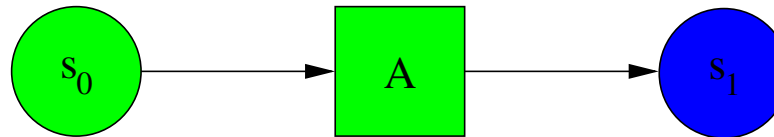
Note:

- transitive closure naturally expressed  
(LP-flavored semantics of  $\mathcal{K}$ )

# Semantics of $\mathcal{K}$ – Principles

transition-based semantics

caused  $fl$  if  $Cond1$  after  $Cond2$



A ... set of actions (executable)

- $Cond2$  is evaluated in  $s_0$ , might include actions.
- $fl$  and  $Cond1$  are evaluated in  $s_1$

Define new state  $s_1$  by a non-monotonic logic program of rules!

$fl :- Cond1$

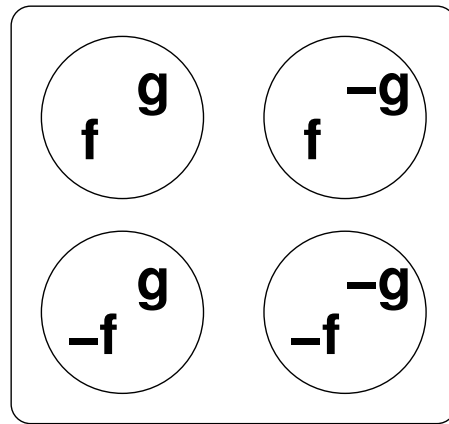
*Remark: several answer sets  $\Leftrightarrow$  several possible succ. states*



# Incomplete states

Usual assumption for action language: total states

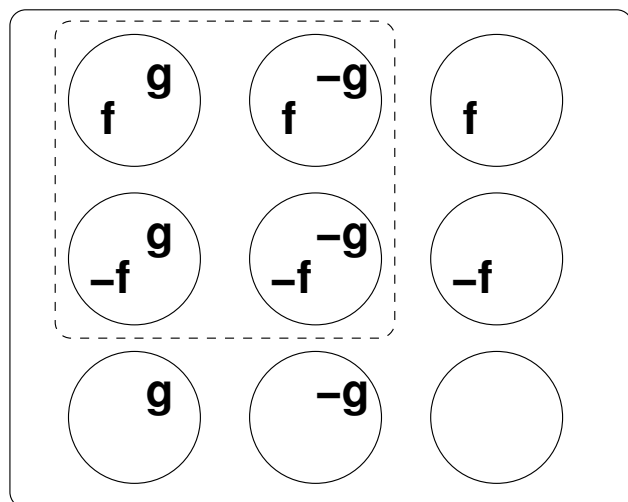
State  $s$  is total  $\Leftrightarrow$  For each fluent  $f$ , either  $f$  or  $\neg f$  must be in  $s$ .



**set of total states for  
the two atoms  $f$  and  $g$**

Total states correspond to total (w.r.t. strong negation!) interpretations

**Incomplete state:** values of some fluents are unknown.



**consistent partial interpretations  
for the two atoms f and g**

Handle incompleteness using principles from nonmonotonic Logic Programming

Note: Differs from Kripke-style  $\mathcal{A}_K$  (Baral & Son, 2001)

# Plans

## Trajectories:

$$T = \langle s_0, A_1, s_1, \dots, s_{n-1}, A_n, s_n \rangle, \quad n \geq 0$$

- $s_0$  is initial state
- each  $s_{i+1}$  is reached by “legal” transition  $s_i, A_{i+1}, s_{i+1}$

## “Optimistic” Plan:

- project  $T$  where  $s_n$  satisfies the goal to  $A_1, A_2, \dots, A_n$

Example:  $P = \text{move}(c, \text{table}); \text{move}(b, a); \text{move}(c, b)$

# Planning under uncertainty in $\mathcal{K}$

- Incomplete states

- Use of default principles: Express “Unknown”

```
executable check_door if not open, not – open.  
forbidden not on(B, L), not – on(B, L).
```

- “Totalize” fluents (case distinction)

```
total on(B, L).
```

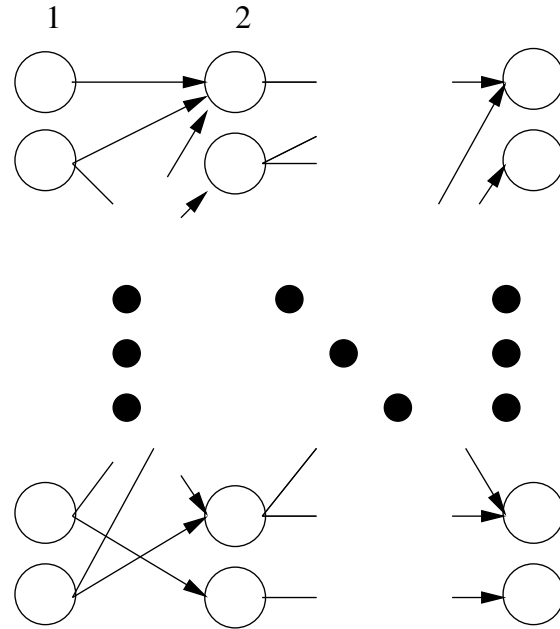
- “secure” plans (= conformant plans)

Always reach the goal by the plan, no matter what happens

- “optimal” plans

action cost declarations, minimize overall cost (not covered here)

# Special Plans – Secure Plans



Trajectories: spanning paths, labels form plans

- **Optimistic Plans:** at least one trajectory to goal
- **Secure Plans:** *each* trajectory from *each* initial state to goal  
no “dead-end” trajectories

# Example: Bomb in the Toilet

$\Pi = \{\text{package}(1). \quad \text{package}(2). \quad \dots \quad \text{package}(p).\}$

fluents : armed(P) requires package(P).

unsafe.

actions : dunk(P) requires package(P).

always : executable dunk(P).

inertial armed(P).

caused – armed(P) after dunk(P).

caused unsafe if armed(P).

initially : total armed(P). % 3 lines: one package is armed

forbidden armed(P), armed(P1), P <> P1.

forbidden not unsafe.

goal : not unsafe ? (p)

**Encodes ALL possible world states!**

# Example: Bomb in the Toilet

$\Pi = \{\text{package}(1). \quad \text{package}(2). \quad \dots \quad \text{package}(p).\}$

fluents :    armed(P) requires package(P).  
             unsafe.

actions :    dunk(P) requires package(P).

always :     executable dunk(P).  
             inertial armed(P).  
             caused – armed(P) after dunk(P).  
             caused unsafe if armed(P).

initially : total armed(P).                    % 3 lines: one package is armed  
             forbidden armed(P), armed(P1), P <> P1.  
             forbidden not unsafe.

goal :        not unsafe ? (p)

**Encodes ALL possible world states!**

Variant: At least one package is armed. What changes?

# Avoiding Totalization

Change view: "unsafe = known that one package is armed"

⇒ "unsafe = not known that all packages are unarmed".

```
fluents :   armed(P) requires package(P).
           unsafe.
actions :   dunk(P) requires package(P).
always :   executable dunk(P).
           inertial  - armed(P).
           caused  - armed(P) after dunk(P).
           caused  unsafe if not - armed(P).
initially :   % tabula rasa, nothing is known
goal :       not unsafe ? (p)
```

**Encodes only what is KNOWN! - Knowledge States**

Single initial state, only det. actions ⇒ need no security check



# Action Language $\mathcal{K}$ - “Forgetting”

Similar to “unknown” fluents in the initial state, we can use knowledge state encodings to “forget” about certain facts by overriding inertia.

Example: non-deterministic “clogging” in Bomb in the toilet.

```
total clogged(T) after flush(T)
inertial -clogged(T) .
```

“The toilet might be clogged or unclogged after being flushed”. “It stays unclogged normally.”

Alternative:

```
inertial -clogged(T) after not flush(T) .
```

“The toilet stays unclogged **unless** it has been flushed”

# Action Language $\mathcal{K}$ - Another example

Avoiding totalization is not always possible: example SQUARE

[Bonet-Geffner, 2000]:

fluents: atX(P) requires index(P). atY(P) requires index(P). anywhere.

actions: up. down. left. right.

always: executable up. executable right. executable left. executable d

nonexecutable up if down. nonexecutable left if right.

inertial atX(X). inertial atY(Y).

caused atX(X) after atX(X1), next(X,X1), left.

caused atX(X1) after atX(X), next(X,X1), right.

caused -atX(X) if atX(X1), X1 != X after atX(X).

[...]

initially: total atX(X). total atY(Y).

forbidden atX(X), atX(X1), X != X1.

forbidden atY(Y), atY(Y1), Y != Y1.

caused anywhere if atX(X), atY(Y).

forbidden not anywhere.

goal: atX(0), atY(0)? (\$n\$)

We can not make use of “unknown” in case of conditional effects.

# Translations to Disjunctive Datalog - The $DLV^{\mathcal{K}}$ Planning System

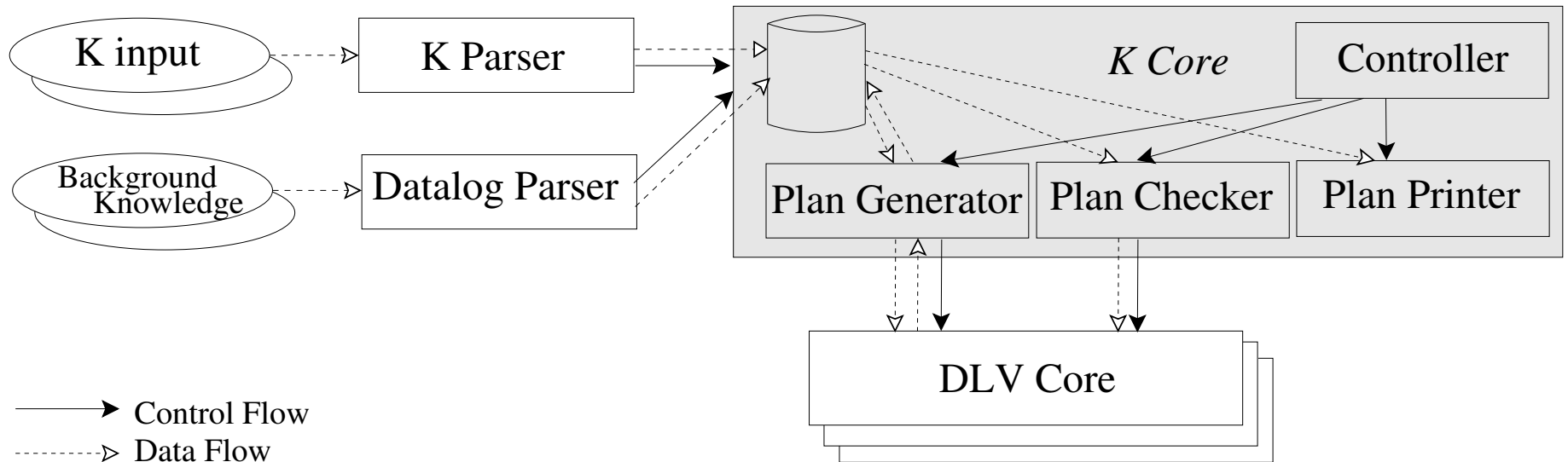


# Translation - Secure check

- Secure planning: Check plan by rewriting this program wrt. plan.
- Hard-code an optimistic plan  $p$  inside the translated program and try to find an answer set where the goal does not hold  $\Pi_{check}(p)$ , or an action of  $p$  is not executable.
- Algorithm for secure planning:
  - compute optimistic plans (i.e. answer sets)
  - Create  $\Pi_{check}$  for optimistic plan) found, if has no answer set, the plan is secure (i.e. conformant).
  - use caching.
- Integrated encodings: cf. [Eiter, Polleres, 2004], [Polleres, 2003]

# DLV<sup>K</sup> System

Architecture:



# Some - old - benchmarks

BMTC( $p, t$ )	steps	DLV <sup>K</sup>		CPLAN	SGP
		$u_s$	$k_s$		
BMTC(2,2)	1	0.02s	0.01s	1.41s	0.95s
BMTC(3,2)	3	0.04s	0.02s	1.50s	3.40s
BMTC(4,2)	3	0.11s	0.03s	1.72s	7.17s
BMTC(5,2)	5	2.79s	0.04s	3.37s	-
BMTC(6,2)	5	37.04s	0.07s	13.04s	-
BMTC(7,2)	7	-	0.52s	71.50s	-
BMTC(8,2)	7	-	10.66s	-	-
BMTC(9,2)	9	-	206.27s	-	-
BMTC(10,2)	9	-	-	-	-
BMTC(2,3)	1	0.02s	0.02s	1.62s	1.15s
BMTC(3,3)	1	0.02s	0.02s	2.31s	1.76s
BMTC(4,3)	3	0.08s	0.03s	4.81s	15.01s
BMTC(5,3)	3	0.35s	0.03s	13.55s	76.28s
BMTC(6,3)	3	17.81s	0.06s	43.34s	592.41s
BMTC(7,3)	5	223.31s	0.13s	210.71s	-
BMTC(8,3)	5	-	0.74s	417.62s	-
BMTC(9,3)	5	-	5.90s	-	-
BMTC(10,3)	7	-	389.08s	-	-
BMTC(2,4)	1	0.02s	0.02s	2.89s	1.52s
BMTC(3,4)	1	0.02s	0.02s	9.19s	2.34s
BMTC(4,4)	1	0.03s	0.02s	37.55s	3.71s
BMTC(5,4)	3	0.18s	0.04s	158.74s	372.74s
BMTC(6,4)	3	5.29s	0.05s	571.77s	-
BMTC(7,4)	3	61.73s	0.09s	-	-
BMTC(8,4)	3	668.74s	0.41s	-	-
BMTC(9,4)	5	-	1.06s	-	-
BMTC(10,4)	5	-	12.14s	-	-

Table 8.6: Experimental results for BMTC( $p$ ), conc. dunks

BMTC( $p, t$ )	steps	DLV <sup>K</sup>		CPLAN	CMBP	GPT
		$u_s$	$k_s$			
BMTC(2,2)	2	0.02s	0.02s	1.41s	0.04s	0.76s
BMTC(3,2)	4	0.07s	0.02s	1.50s	0.05s	0.78s
BMTC(4,2)	6	2.47s	0.04s	1.64s	0.06s	0.81s
BMTC(5,2)	8	208.52s	0.05s	2.66s	0.06s	0.82s
BMTC(6,2)	10	-	0.07s	32.77s	0.09s	0.86s
BMTC(7,2)	12	-	0.10s	12.46s	0.12s	0.96s
BMTC(8,2)	14	-	0.13s	-	0.23s	1.11s
BMTC(9,2)	16	-	0.20s	-	0.48s	1.48s
BMTC(10,2)	18	-	0.28s	-	0.96s	2.26s
BMTC(2,3)	2	0.02s	0.02s	1.50s	0.04s	0.76s
BMTC(3,3)	3	0.03s	0.02s	1.85s	0.04s	0.81s
BMTC(4,3)	5	1.84s	0.03s	2.86s	0.06s	0.84s
BMTC(5,3)	7	291.24s	0.06s	5.92s	0.09s	0.90s
BMTC(6,3)	9	-	0.09s	14.50s	0.14s	0.99s
BMTC(7,3)	11	-	0.25s	40.41s	0.30s	1.17s
BMTC(8,3)	13	-	15.42s	-	0.62s	1.66s
BMTC(9,3)	15	-	-	-	1.44s	2.79s
BMTC(10,3)	17	-	-	-	3.31s	5.64s
BMTC(2,4)	2	0.02s	0.02s	2.02s	0.04s	0.81s
BMTC(3,4)	3	0.41s	0.02s	3.67s	0.05s	0.83s
BMTC(4,4)	4	0.60s	0.03s	9.03s	0.07s	0.92s
BMTC(5,4)	6	149.65s	0.06s	30.55s	0.13s	1.01s
BMTC(6,4)	8	-	0.10s	-	0.23s	1.27s
BMTC(7,4)	10	-	0.15s	199.73s	0.51s	1.85s
BMTC(8,4)	12	-	0.47s	-	1.13s	3.34s
BMTC(9,4)	14	-	67.07s	-	2.94s	7.18s
BMTC(10,4)	16	-	-	-	6.38s	17.34s

Table 8.7: Experimental results for BMTC( $p$ ) sequential

# Conclusions

- Expressive action language, based on principles of LP
- Competitive implementation with suitable encodings (without specialized heuristics (yet)).
- The idea is similar to SAT Planning or CPlan (Castellini, et al. 2001): Translate to a declarative formalism and use existing solvers (`d1v`, `smodels`, etc.).
- Improvements (Magic Sets, Heuristics?), etc.
- Further steps: Integrated encodings, Conditional Planning(?) Plan Repair.



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